## Sketching quadratic graphs

## A LEVEL LINKS

Scheme of work: 1b. Quadratic functions - factorising, solving, graphs and the discriminants

## Key points

- The graph of the quadratic function $y=a x^{2}+b x+c$, where $a \neq 0$, is a curve called a parabola.
- Parabolas have a line of symmetry and

 a shape as shown.
- To sketch the graph of a function, find the points where the graph intersects the axes.
- To find where the curve intersects the $y$-axis substitute $x=0$ into the function.
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- At the turning points of a graph the gradient of the curve is 0 and any tangents to the curve at these points are horizontal.
- To find the coordinates of the maximum or minimum point (turning points) of a quadratic curve (parabola) you can use the completed square form of the function.


## Examples

Example 1 Sketch the graph of $y=x^{2}$.


The graph of $y=x^{2}$ is a parabola.

When $x=0, y=0$.
$a=1$ which is greater than zero, so the graph has the shape:

Example 2 Sketch the graph of $y=x^{2}-x-6$.

When $x=0, y=0^{2}-0-6=-6$
So the graph intersects the $y$-axis at ( $0,-6$ )
When $y=0, x^{2}-x-6=0$
$(x+2)(x-3)=0$
$x=-2$ or $x=3$

So,
the graph intersects the $x$-axis at $(-2,0)$ and (3,0)

1 Find where the graph intersects the $y$-axis by substituting $x=0$.

2 Find where the graph intersects the $x$-axis by substituting $y=0$.
3 Solve the equation by factorising.
4 Solve $(x+2)=0$ and $(x-3)=0$.
$5 a=1$ which is greater than zero, so the graph has the shape:
(continued on next page)

| $x^{2}-x-6=\left(x-\frac{1}{2}\right)^{2}-\frac{1}{4}-6$ | 6To find the turning point, complete <br> the square. |
| :--- | :--- |
| $=\left(x-\frac{1}{2}\right)^{2}-\frac{25}{4}$ | When $\left(x-\frac{1}{2}\right)^{2}=0, x=\frac{1}{2}$ and <br> $y=-\frac{25}{4}$, so the turning point is at the <br> point $\left(\frac{1}{2},-\frac{25}{4}\right)$ <br> The turning point is the minimum <br> value for this expression and occurs <br> when the term in the bracket is <br> equal to zero. |

## Practice

1 Sketch the graph of $y=-x^{2}$.

2 Sketch each graph, labelling where the curve crosses the axes.
a $y=(x+2)(x-1)$
b $\quad y=x(x-3)$
c $\quad y=(x+1)(x+5)$

3 Sketch each graph, labelling where the curve crosses the axes.
a $y=x^{2}-x-6$
b $\quad y=x^{2}-5 x+4$
c $\quad y=x^{2}-4$
d $y=x^{2}+4 x$
e $y=9-x^{2}$
f $\quad y=x^{2}+2 x-3$

4 Sketch the graph of $y=2 x^{2}+5 x-3$, labelling where the curve crosses the axes.

## Extend

5 Sketch each graph. Label where the curve crosses the axes and write down the coordinates of the turning point.
a $y=x^{2}-5 x+6$
b $\quad y=-x^{2}+7 x-12$
c $\quad y=-x^{2}+4 x$

6 Sketch the graph of $y=x^{2}+2 x+1$. Label where the curve crosses the axes and write down the equation of the line of symmetry.

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## Answers

1


2 a

b

b

e

c


C

d

f


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4


5
a
b

c


6


Line of symmetry at $x=-1$.

